



**EUMETSAT**

**AC SAF**

**ATMOSPHERIC COMPOSITION  
MONITORING**

# **PRODUCT USER MANUAL**

## **Near real-time IASI HNO<sub>3</sub>**

### **(O3M-81, O3M-336)**

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1.1	28/04/2022	CDOP-3 was removed from the document and IASI spatial resolution was corrected in Table 5, after RIDs from reviewers.

RELATED PRODUCT LIST

Product ID	Product name	Instrument
O3M-81, O3M-336	IASI NRT HNO3	Metop B, Metop C

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## **1. INTRODUCTION**

### **1.1 Purpose and scope**

This document is the Product User Manual for the Near Real Time IASI HNO<sub>3</sub> retrieved within the context of the Satellite Application Facility on Atmospheric Composition Monitoring (AC SAF). This document gives a brief overview on the IASI retrieval algorithm and explains how to use and interpret the IASI HNO<sub>3</sub> profiles.

This document has been written as FORLI-HNO<sub>3</sub> v20151001\_ sp20171122 was running at EUMETSAT.

### **1.2 Acronyms**

AC SAF: Atmospheric Composition Monitoring Satellite Application Facility

EUMETSAT: European Organisation for the Exploitation of Meteorological Satellites

EUMETCast: EUMETSAT multi-service data dissemination system

WMO: World Meteorological Organization

GTS: Global Telecommunication System

IASI: Infrared Atmospheric Sounding Interferometer

FORLI: Fast Optimal Retrievals on Layers for IASI

ULB: Université Libre de Bruxelles

LATMOS: Laboratoire Atmosphères, Milieux, Observations Spatiales

OEM : Optimal Estimation Method

DOFS : Degrees of Freedom for Signal

CP: Partial Column

TOA: Top Of the Atmosphere

VMR: Volume Mixing Ratio

### **1.3 Applicable and reference documents**

#### **1.3.1 Applicable documents**

[AD1] FORLI Algorithm Theoretical Basis Document SAF/O3M/ULB/FORLI\_ATBD Issue 1, 20/02/2014

[AD2] FORLI-HNO<sub>3</sub> Product Specification, Requirement And Assessment SAF/O3M/ULB/FORLICO\_PSRA Issue 1, 21/01/2015

[AD3] Product Requirements Document SAF/AC/FMI/RQ/PRD/001 Issue 1.6, 25/05/2020

### 1.3.2 Reference documents

- [RD1] Hilton, F.; August, T.; Barnet, C.; Bouchard, A.; Camy-Peyret, C.; Clarisse, L.; Clerbaux, C.; Coheur, P.-F.; Collard, A.; Crevoisier, C.; Dufour, G.; Edwards, D.; Fajjan, F.; Fourrié, N.; Gambacorta, A.; Gauguin, S.; Guidard, V.; Hurtmans, D.; Illingworth, S.; Jacquinet-Husson, N.; Kerzenmacher, T.; Klaes, D.; Lavanant, L.; Masiello, G.; Matricardi, M.; McNally, T.; Newman, S.; Pavelin, E.; Péquignot, E.; Phulpin, T.; Remedios, J.; Schlüssel, P.; Serio, C.; Strow, L.; Taylor, J.; Tobin, D.; Uspensky, A. & Zhou, D. Hyperspectral Earth Observation with IASI. *Bull. Am. Meteorol. Soc.*, 93(3), 347-370, doi: 10.1175/BAMS-D-11-00027.1, 2012.
- [RD2] Camy-Peyret, C. & Eyre, J. The IASI Science Plan. Technical report, A Report From The IASI Sounding Science Working Group, 1998.
- [RD3] Clerbaux, C.; Boynard, A.; Clarisse, L.; George, M.; Hadji-Lazaro, J.; Herbin, H.; Hurtmans, D.; Pommier, M.; Razavi, A.; Turquety, S.; Wespes, C. & Coheur, P. F. Monitoring of atmospheric composition using the thermal infrared IASI/MetOp sounder. *Atmos. Chem. Phys.*, 9(16):6041-6054, 2009.
- [RD4] Rodgers, C.D.. Inverse methods for atmospheric sounding: Theory and Practice, Series on Atmospheric, Oceanic and Planetary Physics - Vol. 2. World Scientific, Singapore, New Jersey, London, Hong Kong, 2000.
- [RD5] Hurtmans, D.; Coheur, P.; Wespes, C.; Clarisse, L.; Scharf, O.; Clerbaux, C.; Hadji-Lazaro, J.; George, M. & Turquety, S. FORLI radiative transfer and retrieval code for IASI. *J. Quant. Spectrosc. Radiat. Transfer*, 113, 1391-1408, 2012.
- [RD6] EUMETCast Dissemination facility  
<http://www.eumetsat.int/website/home/Data/DataDelivery/EUMETCast/index.html>

## **2. INTRODUCTION TO EUMETSAT SATELLITE APPLICATION FACILITY ON ATMOSPHERIC COMPOSITION MONITORING (AC SAF)**

### **Background**

The monitoring of atmospheric chemistry is essential due to several human caused changes in the atmosphere, like global warming, loss of stratospheric ozone, increasing UV radiation, and pollution. Furthermore, the monitoring is used to react to the threads caused by the natural hazards as well as follow the effects of the international protocols.

Therefore, monitoring the chemical composition and radiation of the atmosphere is a very important duty for EUMETSAT and the target is to provide information for policy makers, scientists and general public.

### **Objectives**

The main objectives of the AC SAF is to process, archive, validate and disseminate atmospheric composition products (O<sub>3</sub>, NO<sub>2</sub>, SO<sub>2</sub>, BrO, HCHO, H<sub>2</sub>O, OClO, CO, NH<sub>3</sub>), aerosol products and surface ultraviolet radiation products utilising the satellites of EUMETSAT. The majority of the AC SAF products are based on data from the GOME-2 and IASI instruments onboard Metop satellites.

Another important task besides the near real-time (NRT) and offline data dissemination is the provision of long-term, high-quality atmospheric composition products resulting from reprocessing activities.

### **Product categories, timeliness and dissemination**

*NRT products* are available in less than three hours after measurement. These products are disseminated via EUMETCast, WMO GTS or internet.

- Near real-time trace gas columns (total and tropospheric O<sub>3</sub> and NO<sub>2</sub>, total SO<sub>2</sub>, total HCHO, CO) and ozone profiles
- Near real-time absorbing aerosol indexes from main science channels and polarization measurement detectors
- Near real-time UV indexes, clear-sky and cloud-corrected

*Offline products* are available within two weeks after measurement and disseminated via dedicated web services at EUMETSAT and AC SAF.

- Offline trace gas columns (total and tropospheric O<sub>3</sub> and NO<sub>2</sub>, total SO<sub>2</sub>, total BrO, total HCHO, total H<sub>2</sub>O) and ozone profiles
- Offline absorbing aerosol indexes from main science channels and polarization measurement detectors
- Offline surface UV, daily doses and daily maximum values with several weighting functions

*Data records* are available after reprocessing activities from the EUMETSAT Data Centre and/or the AC SAF archives.

- Data records generated in reprocessing
- Lambertian-equivalent reflectivity
- Total OClO

Users can access the AC SAF offline products and data records (free of charge) by registering at the AC SAF web site.

**More information about the AC SAF project, products and services:** <http://acsaf.org/>

**AC SAF Helpdesk:** [helpdesk@acsaf.org](mailto:helpdesk@acsaf.org)

**Twitter:** [https://twitter.com/Atmospheric\\_SAF](https://twitter.com/Atmospheric_SAF)

### 3. IASI-FORLI RETRIEVAL ALGORITHM

#### 3.1 IASI instrument

IASI is an infrared Fourier transform spectrometer developed jointly by CNES (the French spatial agency) with support of the scientific community (for a review see [RD1]), and by EUMETSAT. IASI is mounted on-board the European polar-orbiting Metop satellite with the primary objective to improve numerical weather predictions, by measuring tropospheric temperature and humidity with high horizontal resolution and sampling, with 1 km vertical resolution, and with respectively 1 K and 10% accuracy [RD2]. IASI also contributes to atmospheric composition measurements for climate and chemistry applications [RD3]. To reach these two objectives, IASI measures the infrared radiation of the Earth's surface and of the atmosphere between  $645$  and  $2760\text{ cm}^{-1}$  at nadir and along a 2200 km swath perpendicular to the satellite track. A total of 120 views are collected over the swath, divided as 30 arrays of 4 individual Field-of-views (FOVs) varying in size from  $36 \times \pi\text{ km}^2$  at nadir (circular 12 km diameter pixel) to  $10 \times 20 \times \pi\text{ km}^2$  at the larger viewing angle (ellipse-shaped FOV at the end of the swath). IASI offers in this standard observing mode global coverage twice daily, with overpass times at around 9:30 and 21:30 mean local solar time. The very good spatial and temporal sampling of IASI is complemented by fairly high spectral and radiometric performances: the calibrated level 1C radiances are at  $0.5\text{ cm}^{-1}$  apodized spectral resolution (the instrument achieves a 2 cm optical path difference), with an apodized noise that ranges below  $2500\text{ cm}^{-1}$  between 0.1 and 0.2 K for a reference blackbody at 280 K [RD1].

#### 3.2 FORLI overview

FORLI (Fast Optimal/Operational Retrievals on Layers for IASI) is a radiative transfer model based on precalculated LUTs capable of processing in near-real-time the numerous radiance measurements made by the high-spatial and high-spectral resolution IASI, with the objective to provide global concentration distributions of atmospheric trace gases. For the inversion step, it relies on a scheme based on the widely used Optimal Estimation theory [RD4]. Three versions of the software have been set-up to process IASI level 1C radiances in near-real-time, for vertical profile retrievals of CO, O<sub>3</sub> and HNO<sub>3</sub>.

The algorithm description with the methods used for forward and inverse modelling is given in the FORLI ATBD [AD1] and in [RD5].

## 4. IASI LEVEL 2 NRT HNO<sub>3</sub> PRODUCT

### 4.1 BUFR PDU file name convention

The names of the IASI Level 2 HNO<sub>3</sub> products distributed on EUMETCast follow this example:  
 W\_XX-EUMETSAT- Darmstadt,SOUNDING+SATELLITE,METOP\*+IASI\_C\_EUM*letter*\_  
 yyyymmddhhmmss\_nnnnn\_eps\_o\_nit\_l2.bin

where:

<i>yyyymmdd</i>	the UTC year, month, day of the data start sensing time
<i>hhmmss</i>	the UTC hour, minute, second of the data start sensing time
<i>nnnnn</i>	the orbit number
<i>*</i>	A, B or C
<i>letter</i>	C for commissioning, P for operational, R for secondary or redundant

### 4.2 BUFR file size estimate

The size of the output may vary and is on average 1 Mb with a number of 480 files per day per instrument.

### 4.3 Description of the content of the BUFR PDU file

The IASI Level 2 HNO<sub>3</sub> BUFR PDU file structure is summarised below. The FORLI-HNO<sub>3</sub> product is provided in the last 11 fields (in bold).

Table 1: Data descriptors of IASI Level 2 HNO<sub>3</sub> BUFR file

#	DATA DESCRIPTOR		NAME USED HEREAFTER
0	0-0-1007	SATELLITE IDENTIFIER	
1	0-0-1031	IDENTIFICATION OF ORIGINATING/GENERATING CENTRE	
2	0-25-060	SOFTWARE IDENTIFICATION	
3	0-0-2019	SATELLITE INSTRUMENTS	
4	0-0-2020	SATELLITE CLASSIFICATION	
5	0-0-4001	YEAR	
6	0-0-4002	MONTH	
7	0-0-4003	DAY	
8	0-0-4004	HOUR	
9	0-0-4005	MINUTE	
10	0-0-4006	SECOND	
11	0-0-5040	ORBIT NUMBER	
12	2-0-1133	#N/A	



13	0-0-5041	SCAN LINE NUMBER	
14	2-0-1000	#N/A	
15	0-0-5001	LATITUDE (HIGH ACCURACY)	
16	0-0-6001	LONGITUDE (HIGH ACCURACY)	
17	0-0-5043	FIELD OF VIEW NUMBER	
18	0-0-7024	SATELLITE ZENITH ANGLE	
19	0-0-5021	BEARING OR AZIMUTH (DEGREE TRUE)	
20	0-0-7025	SOLAR ZENITH ANGLE	
21	0-0-5022	SOLAR AZIMUTH (DEGREE TRUE)	
22	0-0-7007	HEIGHT (Surface altitude in meter)	
23	0-0-8046	ATMOSPHERIC CHEMICAL OR PHYSICAL CONSTITUENT TYPE	
24	0-4-0056	GENERAL RETRIEVAL QUALITY FLAG	HNO3_QFLAG
25	0-4-0058	NUMBER OF VECTORS DESCRIBING THE CHAR. MATRICES	HNO3_NPCA
26	0-4-0059	NUMBER OF LAYERS ACTUALLY RETRIEVED	HNO3_NFITLAYERS
27	0-4-0060	NUMBER OF HNO3 PROFILES RETRIEVED IN SCANLINE	HNO3_NBR
28	0-4-0054	POTENTIAL PROCESSING AND INPUTS ERRORS	HNO3_BDIV_LO
29	0-4-0055	DIAGNOSTICS ON THE RETRIEVAL	HNO3_BDIV_HI
30	1-0-5041	#N/A REPEAT NEXT 5 41 TIMES	
31	0-4-0061	AIR PARTIAL COLUMNS ON EACH RETRIEVED LAYER	HNO3_CP_AIR
32	2-0-2131	#N/A	
33	0-4-0062	A-PRIORI PARTIAL COLUMNS FOR HNO3 ON EACH RETRIEVED LAYER	HNO3_CP_HNO3_A
34	2-0-2000	#N/A	
35	0-4-0063	SCAL. VEC. MULT. A-PRI. HNO3 VEC. DEF. RETR. HNO3 VEC.	HNO3_X_HNO3
36	1-0-1021	#N/A REPEAT NEXT 1 21 TIMES	
37	0-4-0064	MAIN EIGENVALUES OF THE SENSITIVITY MATRIX	HNO3_H_EIGENVALUES
38	1-0-2215	#N/A REPEAT NEXT 2 215 TIMES	
39	1-0-1004	#N/A REPEAT NEXT 1 4 TIMES	
40	0-4-0065	MAIN EIGENVECTORS OF THE SENSITIVITY MATRIX	HNO3_H_EIGENVECTORS

**Usual FORLI-HNO<sub>3</sub> products have to be reconstructed/calculated from these above mentioned fields, see Section 5.**

Among the other IASI Level 2 available products, temperature, humidity and cloud information needed to completely characterize FORLI-HNO<sub>3</sub> products can be found in files distributed by EUMETCast called:



W\_XX-EUMETSAT- Darmstadt,SOUNDING+SATELLITE,METOP\*+IASI\_C\_EUM*letter*\_yyyymmddhhmmss\_nnnnn\_eps\_o\_<prod>\_l2.bin

where:

<i>yyyymmdd</i>	the UTC year, month, day of the data start sensing time
<i>hhmmss</i>	the UTC hour, minute, second of the data start sensing time
<i>nnnnn</i>	the orbit number
<i>*</i>	A, B or C
<i>letter</i>	C for commissioning, P for operational, R for secondary or redundant

product code <prod>	
twt	atmospheric temperature and water vapour
clp	cloud parameters

## 5. THE FORLI-HNO<sub>3</sub> PRODUCT

### 5.1 Product description

The product FORLI-HNO<sub>3</sub> includes several variables, described in Table 1 (bold) and in Table 2. The principal product is a vertical profile of HNO<sub>3</sub> provided on 41 layers, from the ground to 40 km with an additional layer from 40 km to TOA. In order to allow a rational use each retrieved profile is associated with averaging kernels and posterior error covariance matrices following the characterization of the optimal estimation. **For saving space, the matrices are compressed and have to be reconstructed using eigenvectors and eigenvalues of the sensitivity matrix (“MAIN EIGENVECTORS OF THE SENSITIVITY MATRIX” and “MAIN EIGENVALUES OF THE SENSITIVITY MATRIX”).** Each retrieval has also associated retrieval flags.

Note that the retrievals are performed on the basis of the *a priori* partial columns (“A-PRIORI PARTIAL COLUMNS FOR HNO<sub>3</sub> ON EACH RETRIEVED LAYER” called hereafter *HNO<sub>3</sub>\_CP\_HNO<sub>3</sub>\_A*), which are scaled individually using a *multiplication factor* (“SCAL. VEC. MULT. A-PRI. HNO<sub>3</sub> VEC. DEF. RETR. HNO<sub>3</sub> VEC” called hereafter *HNO<sub>3</sub>\_X\_HNO<sub>3</sub>*). The multiplication factor equals therefore 1 at initial stage, is unitless, and should remain close to unity in normal circumstances. This ensures homogeneity of the retrieved values all along the altitudes, even when molecular amounts spans several decades. The content of *HNO<sub>3</sub>\_CP\_HNO<sub>3</sub>\_A* is computed using ray tracing methods described in the ATBD [AD1], while *HNO<sub>3</sub>\_X\_HNO<sub>3</sub>* is retrieved using OEM method in a logarithmic space in order to avoid nonphysical negative values.

Table 2: Description and units of FORLI-HNO<sub>3</sub> product available in the IASI L2 HNO<sub>3</sub> BUFR files

Name	Description	Units
<b>HNO<sub>3</sub>_QFLAG</b>	General quality flag	N/A
<b>HNO<sub>3</sub>_BDIV_LO</b>	Potential processing and input errors	N/A
<b>HNO<sub>3</sub>_BDIV_HI</b>	Diagnostics on the retrieval	N/A
<b>HNO<sub>3</sub>_NPCA</b>	Number of vectors describing the characterization matrices	N/A
<b>HNO<sub>3</sub>_NFITLAYERS</b>	Number of layers actually retrieved; ≤ 41	N/A
<b>HNO<sub>3</sub>_NBR</b>	Number of HNO <sub>3</sub> profiles retrieved in scanline	N/A
<b>HNO<sub>3</sub>_CP_AIR</b>	Air partial column on each retrieved layer	moles /cm <sup>2</sup>
<b>HNO<sub>3</sub>_CP_HNO<sub>3</sub>_A</b>	A priori partial columns for HNO <sub>3</sub> on each retrieved layer	moles /cm <sup>2</sup>
<b>HNO<sub>3</sub>_X_HNO<sub>3</sub></b>	Scaling vector multiplying the a priori HNO <sub>3</sub> vector in order to define the retrieved HNO <sub>3</sub> vector	N/A
<b>HNO<sub>3</sub>_H_EIGENVALUES</b>	Main eigenvalues of the sensitivity matrix	N/A
<b>HNO<sub>3</sub>_H_EIGENVECTORS</b>	Main eigenvectors of the sensitivity matrix	N/A

In Table 2 HNO<sub>3</sub>\_QFLAG is a single code assessing the quality of the retrieved profiles namely 2 for best quality pixels, 1 for valuable pixels and 0 for bad quality pixels. HNO<sub>3</sub>\_QFLAG is a FORLI-HNO<sub>3</sub> output, see Section 5.3.1.

Table 3a: Potential processing and inputs errors in FORLI-HNO<sub>3</sub> (HNO<sub>3</sub>\_BDIV\_LO). Note that old bits have been reassigned with new WMO descriptor bits.

Name	Value	old Bit	WMO bit	Description	Comment
<b>General</b>					
AMP_ERROR	1	0	1	An error has been detected	
<b>Origin</b>					
AMP_L1	2	1	2	Message from L1	
AMP_L2	4	2	3	Message from L2	
AMP_ANC	8	3	4	Message from ancillary data	
AMP_FIT	16	4	5	Message from fitting procedure	
<b>Input content</b>					
AMP_QUALFLAG	256	8	7	Quality flag	Either bad L1 (qFlag) or L2 (F_IASI_Bad) flag raised
AMP_LINREG_L2	512	9	8	Level 2 "from linear regression" (F_Qual), report a pixel where L2 are not fully trusted	
AMP_EMPTY	1024	10	9	Empty field or data	Indicate missing T or humidity level(s) in the vertical profile
AMP_INCOMPLETE	2048	11	10	Missing surface pressure value	

Table 3b: Diagnostics on the retrieval of FORLI-HNO<sub>3</sub> (HNO<sub>3</sub>\_BDIV\_HI). Note that old bits have been reassigned with new WMO descriptor bits.

Name	Value	old Bit	WMO bit	Description	Comment
<b>Filtering</b>					
AMP_RADFILTER	4096	12	11	Radiance filtering	Not used in this context
AMP_POLES	8192	13	12	Polar regions	Not used in this context
AMP_NIGHT	16384	14	13	Location in the night	Not used in this context
AMP_NEGZO	32768	15	14	Negative altitude	Surface below m.s.l.
AMP_COVERAGE	65536	16	15	Cloud covered scene	
AMP_SEA	131072	17	16	Scene above the sea	Not used so far
AMP_DESERT	262144	18	17	Scene above desert	
AMP_TSKIN	524288	19	18	Skin temperature	Missing skin temperature, start from BT
AMP_TDIFF	1048576	20	19	Skin temperature differential	Retrieved skin T too different from model
AMP_CONTRAST	2097152	21	20	Spectral line contrast too weak	No lines seen on spectrum (polar regions)
<b>Fitting</b>					
AMP_ITERATIONS	4194304	22	21	Maximum number of iterations exceeded	
AMP_NEGPC	8388608	23	22	Negative partial columns	
AMP_CONDITION	16777216	24	23	Matrix ill conditioned	
AMP_DIVERGED	33554432	25	24	Fit diverged	
AMP_GSL	67108864	26	25	Error in gsl usage	
AMP_BIAS	134217728	27	26	Residuals "biased"	
AMP_SLOPE	268435456	28	27	Residuals "sloped"	
AMP_RMS	536870912	29	28	Residuals rms large	
AMP_AVK	1073741824	30	29	Weird averaging kernels	
AMP_ICE	2147483648	31	30	Ice presence detected	

## 5.2 How to get the FORLI-HNO<sub>3</sub> products I need?

Table 4: FORLI-HNO<sub>3</sub> products that can be obtained from the BUFR PDU files.

FORLI-HNO <sub>3</sub> products	Notation	How to get/calculate it?	From
HNO <sub>3</sub> profile (moles/cm <sup>2</sup> )	HNO3_CP_HNO3	see Section 5.2.1, Eq 1	nit
HNO <sub>3</sub> profile (VMR)	HNO3_VMR_HNO3	see Section 5.2.1, Eq 2	
HNO <sub>3</sub> total column (moles/cm <sup>2</sup> )	HNO3_TC	see Section 5.2.1, Eq. 3	
A priori profile (moles/cm <sup>2</sup> )	HNO3_CP_HNO3_A	Field "A-PRIORI PARTIAL COLUMNS FOR HNO <sub>3</sub> ON EACH RETRIEVED LAYER"	
A priori profile (VMR)	HNO3_VMR_HNO3_A	See Section 5.2.3.2, Eq 10	
Averaging Kernel matrix in scaling factor	A	see Section 5.2.2, Eq.6	
Averaging Kernel matrix in partial column	A <sub>PC</sub>	see Section 5.2.3.1, Eq. 9	
Averaging Kernel matrix in VMR	A <sub>VMR</sub>	see Section 5.2.3.2, Eq. 12	
Total column averaging kernel vector	k	See Section 5.2.3.3, Eq. 13	
Degrees Of Freedom of the Signal	DOFS	trace(A) = trace(A <sub>PC</sub> ) = trace(A <sub>VMR</sub> )	
Absolute total retrieval error on the total column	σ <sub>TC</sub>	See Section 5.2.3.3, Eq. 14	
Relative error profile (relative to the retrieved HNO <sub>3</sub> profile in moles/cm <sup>2</sup> or VMR)	σ	See Section 5.2.2, Eq. 7	
Pressure levels	p	See Section 5.2.3.4, Eq. 16 to 18	twf

### 5.2.1 Reconstruction of the HNO<sub>3</sub> profile and calculation of the total column

The final **partial column profile** (moles/cm<sup>2</sup>) is to be reconstructed by multiplying element-wise the two vectors defined earlier e.g.:

$$HNO3\_CP\_HNO3_i = HNO3\_CP\_HNO3\_A_i \times HNO3\_X\_HNO3_i \quad \forall i \quad (1)$$

Profile spans *HNO3\_NFITLAYERS* layers, sampled on a 1 km grid, except the first one which starts from surface altitude and hence could be thinner, and the last one which extends up to TOA.

To convert this profile in VMR:

$$HNO3\_VMR\_HNO3_i = HNO3\_CP\_HNO3_i \div HNO3\_CP\_AIR_i \quad \forall i \quad (2)$$

The **HNO<sub>3</sub> total column** (moles cm<sup>-2</sup>) is obtained by summing the partial columns defined in Eq (1) on all retrieved layers:

$$HNO3\_TC = \sum_i HNO3\_CP\_HNO3_i \quad (3)$$

The total (or partial columns) can be similarly expressed in molecules cm<sup>-2</sup> by multiplying the values in moles cm<sup>-2</sup> by  $6.02214086 \times 10^{+23}$ .

### 5.2.2 Reconstruction of the characterisation matrices

Averaging kernel, which is normally an asymmetric matrix (*HNO3\_NFITLAYERS* × *HNO3\_NFITLAYERS*), is compressed by using a principal component decomposition representation. A reduced subset of principal vectors (*HNO3\_NPCA* out of *HNO3\_NFITLAYERS*) of the sensitivity matrix, *H*, is retained in order to achieve a meaningful compression. The averaging kernel matrix, *A*, is then reconstructed. The posterior variance-covariance matrix is also rebuilt during this procedure. Reconstruction is done using the following formulation:

$$H = v \text{diag}(\lambda) v^T \quad (4)$$

$$\hat{S} = (H + S_a^{-1})^{-1} \quad (5)$$

$$A = \hat{S}H \quad (6)$$

where:

*v* is the principal eigenvectors matrix (*HNO3\_NFITLAYERS* × *HNO3\_NPCA*);

*λ*, the principal eigenvalues vector (*HNO3\_NPCA* × *HNO3\_NPCA*);

*S<sub>a</sub>*, the *a priori* variance-covariance matrix;

*Ŝ*, the posterior variance-covariance matrix;

*A*, the averaging kernels matrix;

and *diag* constructs a diagonal matrix the elements of which are given by the parameter vector.

When the surface altitude > 1 km (i.e. *HNO3\_NFITLAYERS* < 41), users have to be careful and reduce *S<sub>a</sub>* accordingly by decimating the first rows/columns corresponding to the unused altitude layers.

Eigenvectors matrix *v* is the *HNO3\_H\_EIGENVECTORS* linear entry properly reshaped, and eigenvalues vector *λ* is the *HNO3\_H\_EIGENVALUES* entry.

The *a priori* variance-covariance matrix  $S_a$  needed for the reconstruction is provided in Section 6.1.

Then the relative error profile can be calculated:

$$\sigma_i = \frac{\sqrt{\hat{S}_{i,i}}}{HNO3\_X\_HNO3_i} \quad \forall i \quad (7)$$

As it is relative to the retrieval, the relative error profile is the same for the retrieved  $HNO_3$  profile in moles/cm<sup>2</sup> or VMR. It has therefore not to be recalculated.

A Python reading routine that reconstruct  $H$ ,  $\hat{S}$  and  $A$  is given in Section 6.2.

Reconstruction follows the same procedure as for CO using adapted vectors and matrices dimensions of 41 and 41x41 respectively. Due to the overwhelming size of such a document, they will not be given here. Users willing to have an example adapted for  $O_3$  and/or  $HNO_3$  can have them on request.

### 5.2.3 Unit conversions

All computations made in Section 5.2.2 were done in the unitless space of the multiplication factor. Users wishing to change the unit space should apply the following conversion rules:

#### 5.2.3.1 Partial columns (moles/cm<sup>2</sup>)

Partial column being defined by equation 1, it is easy to demonstrate that:

$$\hat{S}_{PC} = \text{diag}(HNO3\_CP\_HNO3\_A) \hat{S} \text{diag}(HNO3\_CP\_HNO3\_A) \quad (8)$$

$$A_{PC} = \text{diag}(HNO3\_CP\_HNO3\_A) A \text{diag}(HNO3\_CP\_HNO3\_A)^{-1} \quad (9)$$

#### 5.2.3.2 Volume mixing ratios

Average volume mixing ratios (VMR) of the layers are computed as the ratios of the partial columns by the corresponding air partial columns. These latter are provided as  $HNO3\_CP\_AIR$ . Hence conversions are given by:

$$HNO3\_VMR\_HNO3\_A_i = HNO3\_CP\_HNO3\_A_i / HNO3\_CP\_AIR_i \quad \forall i \quad (10)$$

$$\hat{S}_{VMR} = \text{diag}(HNO3\_VMR\_HNO3\_A) \hat{S} \text{diag}(HNO3\_VMR\_HNO3\_A) \quad (11)$$

$$A_{VMR} = \text{diag}(HNO3\_VMR\_HNO3\_A) A \text{diag}(HNO3\_VMR\_HNO3\_A)^{-1} \quad (12)$$

#### 5.2.3.3 Total columns

The total column averaging kernel vector ( $k$ ) is obtained by summing the rows of the averaging kernel matrix  $A$ :



$$k = (k_1 \ k_2 \ \dots \ k_{O_3\_NFITLAYERS}),$$

with  $k_i = A_{1,i} + A_{2,i} + \dots + A_{O_3\_NFITLAYERS,i}$ ,  $i=1$  to HNO<sub>3</sub>\_NFITLAYERS, (13)

The absolute total retrieval error (in moles/cm<sup>2</sup>) on the total column is then calculated as  $\sigma_{TC}$

$$\sigma_{TC} = \sqrt{\sum_{i,j} \hat{S}_{PC_{i,j}}}$$
 (14)

#### 5.2.3.4 Altitude-pressure conversion

Temperature and humidity vertical profiles extracted from **IASI L2 twt product** are given on 101 pressure levels (in Pa). To calculate the pressure levels corresponding to the altitude levels of the FORLI-HNO<sub>3</sub> retrievals, one should first calculate the altitude levels corresponding to the IASI L2 twt product.

From temperature and humidity vertical profiles (extracted from IASI L2 twt product), the correspondence between altitude and pressure could be calculated by iterating from the surface to the top of the atmosphere. The assumptions on the surface characteristics are:

surface altitude =  $z_0$  (“HEIGHT”, from BUFR files)

surface pressure =  $p_0$  (“PRESSURE (HIGH PRECISION)” from IASI L2 twt product)

surface temperature =  $T_0$ , first level of the temperature profile T (extracted from IASI L2 twt product)

surface humidity =  $q_0$ , first level of the humidity profile q (extracted from IASI L2 twt product)

The acceleration due to the gravity is function of the geographic latitude  $\phi$  and of the altitude  $z_i$ :

$$g(z_i, \phi) = g_\phi - (3.085462 \times 10^{-6} + 2.27 \times 10^{-9} \cos(2\phi))z_i + (7.254 \times 10^{-13} + 1.0 \times 10^{-20} \cos(2\phi))z_i^2 - (1.517 \times 10^{-19} + 6 \times 10^{-22} \cos(2\phi))z_i^3$$
 (15)

where

$$g_\phi = 9.806160(1 - 0.0026373 \cos(2\phi) + 0.0000059 \cos^2(2\phi)) \text{ ms}^{-2}$$
 (16)

The mean virtual temperature between two pressure levels  $p_i$  and  $p_{i+1}$  (just above level  $i$ ) is then:

$$\overline{T_{v_{l,i+1}}} = \frac{T_i(1+0.608 q_i) + T_{i+1}(1+0.608 q_{i+1})}{2}$$
 (17)

with  $T_i$  and  $q_i$ , the temperature and humidity at  $p_i$ , respectively, and  $T_{i+1}$  and  $q_{i+1}$ , the temperature and humidity at  $p_{i+1}$ , respectively.

Then the altitude of the pressure level  $p_{i+1}$  can be estimated from the pressure level  $p_i$  (just below level  $i+1$ ):

$$z_{i+1} = z_i + \frac{R \times \overline{T_{v_{l,i+1}}}}{g(z_i, \phi)} \times \ln \frac{p_i}{p_{i+1}}$$
 (18)

with  $R = 287.06 \text{ JK}^{-1}\text{kg}^{-1}$ , the gas constant for dry air



We obtain the altitude profile corresponding to the IASI L2 twt product. Then we can extract the pressure levels associated to IASI FORLI-HNO<sub>3</sub> product from the pressure vertical profile by using a cubic spline interpolation.

The conversion between pressure and altitude is done as in the “IASI Level2 Product Generation specification” document.

## 5.3 Using the product

### 5.3.1 Quality Flags for the retrieved profile

HNO<sub>3</sub>\_QFLAG is a single code assessing the quality of FORLI retrieved HNO<sub>3</sub> total column. HNO<sub>3</sub>\_QFLAG is a FORLI-HNO<sub>3</sub> output. It can be 2 (best quality), 1 (acceptable quality) or 0 (the rest).

HNO<sub>3</sub>\_QFLAG=2 for the most reliable pixels, in other words the best quality pixels. Unused so far, but reserved for future versions.

HNO<sub>3</sub>\_QFLAG=1 for the valuable pixels, to use with caution, *calculated as*:

- total cloud cover <25%
- flags  
AMP\_ERROR+AMP\_EMPTY+AMP\_INCOMPLETE+AMP\_TDIFF+AMP\_ITERATION  
S+AMP\_NEGPC + AMP\_CONDITION+ AMP\_DIVERGED +AMP\_AVK are null (see Table 3b)
- RMS (residual rms)<3.0e-8
- DOFS>0.9
- -0.6e-9<BIAS (residual biased)<0.4e-9

HNO<sub>3</sub>\_QFLAG=0 for the remaining pixels. We recommend not using these pixels.

For data validation or assimilation purposes, we recommend using the data with HNO<sub>3</sub>\_QFLAG equal to 1 for the moment.

## 5.4 Accuracy of the product

The requirements of the product are given in terms of threshold, target and optimal values in Table 5 below. This information is taken from the FORLI-HNO<sub>3</sub> product specification, requirement and assessment document [AD2] and is also given in the Product Requirements Document [AD3].

Table 5: FORLI-HNO<sub>3</sub> product requirements.

Error* (%)			Spatial resolution	Spatial coverage	Cloud fraction	NRT
Threshold	Target	Optimal				
50%	35%	10%	IASI spatial resolution	Global	< 25 %	< 3h

\*difference of quantity value obtained by measurement and true value of the quantity intended to be measured, as defined by CEOS/ISO:19159 (ISO/TS 19159-1:2014(en), Geographic information - Calibration and validation of remote sensing imagery sensors and data — Part 1: Optical sensors).

## 5.5 Validation of the product

The validation of the FORLI-HNO<sub>3</sub> product is performed at BIRA (Belgian Institute for Space Aeronomy).

## 5.6 Product dissemination and archiving

### 5.6.1 Near real time Product dissemination

The IASI Level 2 products are disseminated to users in near real-time through EUMETCast [RD6] with a time lapse of two hours from sensing to delivery. The data is disseminated in WMO (BUFR) format. A full description of the IASI HNO<sub>3</sub> Level 2 BUFR content is given in Section 4.3.

### 5.6.2 Archive retrieval

The IASI Level 2 products available from the EUMETSAT Data Centre are archived as full-dump products, but sub-setting capabilities are provided to the user in the retrieval process. The products in the EUMETSAT Data Centre are available to users for eight to nine hours after sensing, either in EPS native, in BUFR or in NetCDF format.

## 6. APPENDICES

### 6.1 A priori variance-covariance matrix $S_a$ used in the FORLI-HNO<sub>3</sub> algorithm

```
Sa_HNO3=matrix[+2.58543354e+00,+1.89875600e+00,+1.49824985e+00,+1.06784122e+00,+7.27450721e-01,+6.61017970e-01,+5.45216295e-01,+4.34912674e-01,+3.31813966e-01,+2.08499112e-01,+1.22909887e-01,+1.32476484e-02,-6.41369861e-02,-1.27798829e-01,-1.60811331e-01,-1.77138159e-01,-4.96961582e-04,-1.16757090e-03,-7.01891783e-04,-2.69775973e-04,+3.08481559e-04,+4.23792981e-04,+6.02237257e-04,+8.34627528e-04,+8.49442127e-04,+7.86094906e-04,+7.20648514e-04,+8.11073298e-04,+9.13567404e-04,+1.26497646e-03,+1.83075080e-03,+1.67378643e-03,+1.25504177e-03,+1.69721187e-03,+1.85810659e-03,+1.46306696e-03,+4.40862903e-04,-2.23276153e-04,+8.61791022e-04,+1.40415266e-03,+1.40415266e-03;  
...  
+1.89875600e+00,+1.72082490e+00,+1.47472039e+00,+1.05013164e+00,+6.65760518e-01,+5.95399926e-01,+4.75905062e-01,+3.67474165e-01,+2.91780743e-01,+1.65627783e-01,+8.26485401e-02,-3.47213379e-02,-1.05868895e-01,-1.66602619e-01,-1.84859287e-01,-1.87348544e-01,-4.09357189e-02,-2.44733747e-02,-1.54089520e-02,-9.56482645e-03,-6.65050399e-03,-3.93400321e-03,-2.60427609e-03,-2.29854103e-03,-1.53118172e-03,-3.58734051e-04,+1.00020845e-03,+1.96278661e-03,+2.53895644e-03,+1.77091771e-03,-1.24320683e-04,+3.08541727e-04,+1.88503399e-03,+2.80681655e-04,-3.04094471e-04,+1.12718776e-03,+4.83991275e-03,+7.25947370e-03,+3.31923139e-03,+1.34197119e-03,+1.34197118e-03;  
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+1.49824985e+00,+1.47472039e+00,+1.35196779e+00,+1.00526036e+00,+6.31720829e-01,+5.60866205e-01,+4.46709991e-01,+3.50776817e-01,+2.69184890e-01,+1.56535583e-01,+7.85022674e-02,-2.59642240e-02,-9.31855683e-02,-1.46224818e-01,-1.65286932e-01,-1.71125732e-01,-4.44643746e-02,-2.99984054e-02,-1.88792772e-02,-1.13260236e-02,-6.48026461e-03,-3.94093646e-03,-2.62752927e-03,-2.11181791e-03,-1.88328418e-03,-1.53378416e-03,-7.88107894e-04,+5.53236097e-04,+1.70510194e-03,+2.60062681e-03,+3.13640587e-03,+2.18046113e-03,+1.45911542e-03,+2.25185988e-03,+2.53894667e-03,+1.83064649e-03,-1.61335150e-06,-1.19948790e-03,+7.52956925e-04,+1.72396881e-03,+1.72396881e-03;  
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## 6.2 Reading routines in Python to reconstruct H, S and A

```
#!/usr/bin/python
#-*- coding:utf-8 -*-

## This script read the compressed H matrix (eigenvalues and eigenvectors) for two cases from the file 'NIT.inp'
## normally these will be read from the Forli HNO3 products (HNO3_H_EIGENVALUES and
HNO3_H_EIGENVECTORS)

## It then reconstructs H and show how to compute the retrieval error covariance matrix, S, and the
## averaging kernel, A

import sys
from numpy import *
from numpy.linalg import *

from Sa_HNO3 import * ## Get the apriori error covariance matrix Sa

line_type=0
with open('NIT.inp','r') as f:
    for line in f:
        if line[0]!='#':
            comment=line.replace("\n", " ")
            continue
        if line_type==0:
            E=fromstring(line,dtype=float, sep=',') ## E (HNO3_H_EIGENVALUES)
            line_type=1
        elif line_type==1:
            V=fromstring(line,dtype=float, sep=',') ## V (HNO3_H_EIGENVECTORS)
            line_type=2
        if line_type==2:
            line_type=0

    nEvals=sum(isfinite(E)) # number of eigenvalues/eigenvectors (of H)
    nEvecs=sum(isfinite(V)) # total number of elements in the eigenvectors (of H)
    nAlts=nEvecs/nEvals # length of each eigenvector (i.e. number of altitudes)
    nSkip=int(41-nAlts)

    E=E[:nEvals]
    V=V[:nEvecs].reshape((nEvals,nAlts))

    ## H = V'EV (reconstruct H from eigendecomposition)
    H=dot(dot(V.T,diag(E)),V)

    Sa_Local=Sa[nSkip:nSkip:] # skip altitudes below surface from Sa, the apriori error covariance matrix

    ## S = (H + Sa^-1)^-1 (retrieval error covariance matrix)
    S=inv(H+inv(Sa_Local))

    ## A = SH (averaging kernel)
    A=dot(S,H)

    print(comment)
    print("S = ",S)
    print("A = ",A)
    print("DOFS = ",trace(A))
```

---